On univalent functions defined by a generalized Sălăgean operator

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FEKETE-SZEGÖ PROBLEM FOR SOME SUBCLASSES OF HOLOMORPHIC FUNCTIONS DEFINED BY THE COMBINATION OF OPOOLA AND BABALOLA DIFFERENTIAL OPERATORS

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Abstract. Inspired by the recent works of Çağlar and Orhan [5] and Kanas and Darwish [12], we obtain the coefficient estimates and Fekete-Szegö inequalities for some new subclasses of holomorphic functions defined by the combination of Opoola and Babalola differential operators.

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